

Sketched RT3D: How to Reconstruct Billions of Photons Per Second

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Single-photon lidar

Pixelwise observation model

$$\pi(x_p | \alpha, t) = \sum_{k=1}^K \alpha_k \pi_s(x_p | t_k) + \alpha_0 \pi_b(x_p)$$

DEPTHS
 # SURFACES PER PIXEL
 BACKGROUND DISTRIBUTION
 TIME-OF-ARRIVAL PTH PHOTON
 REFLECTIVITIES
 SIGNAL DISTRIBUTION

Spatial regularization

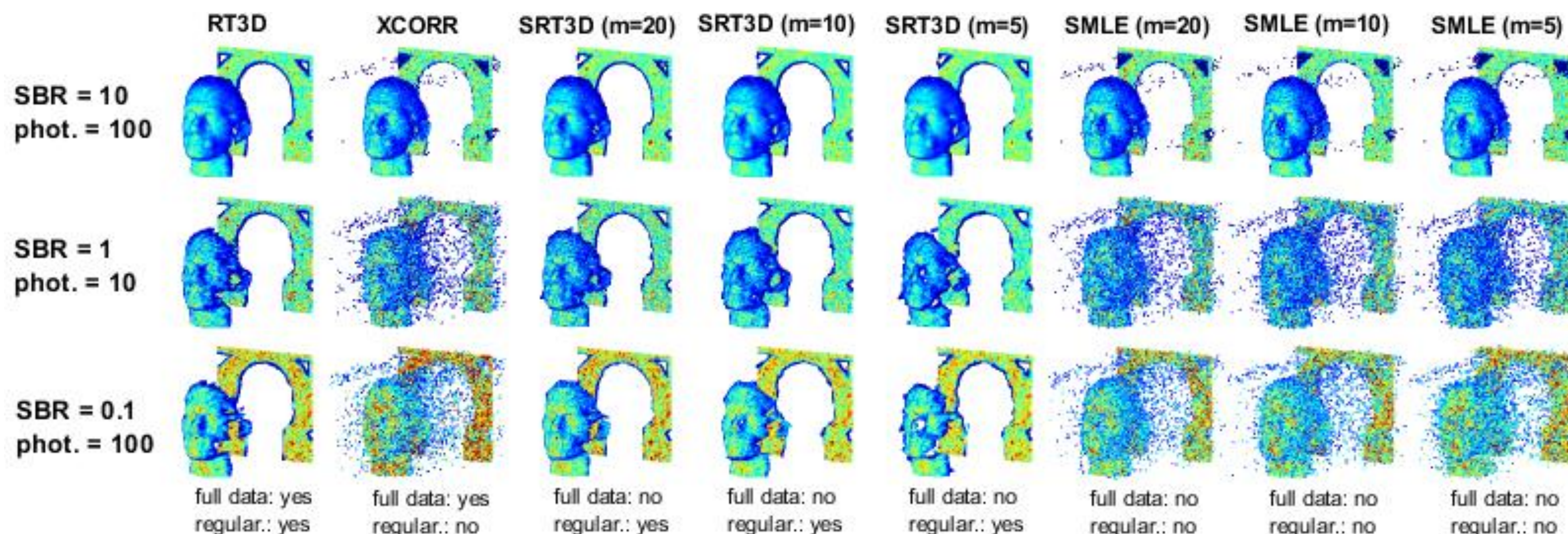
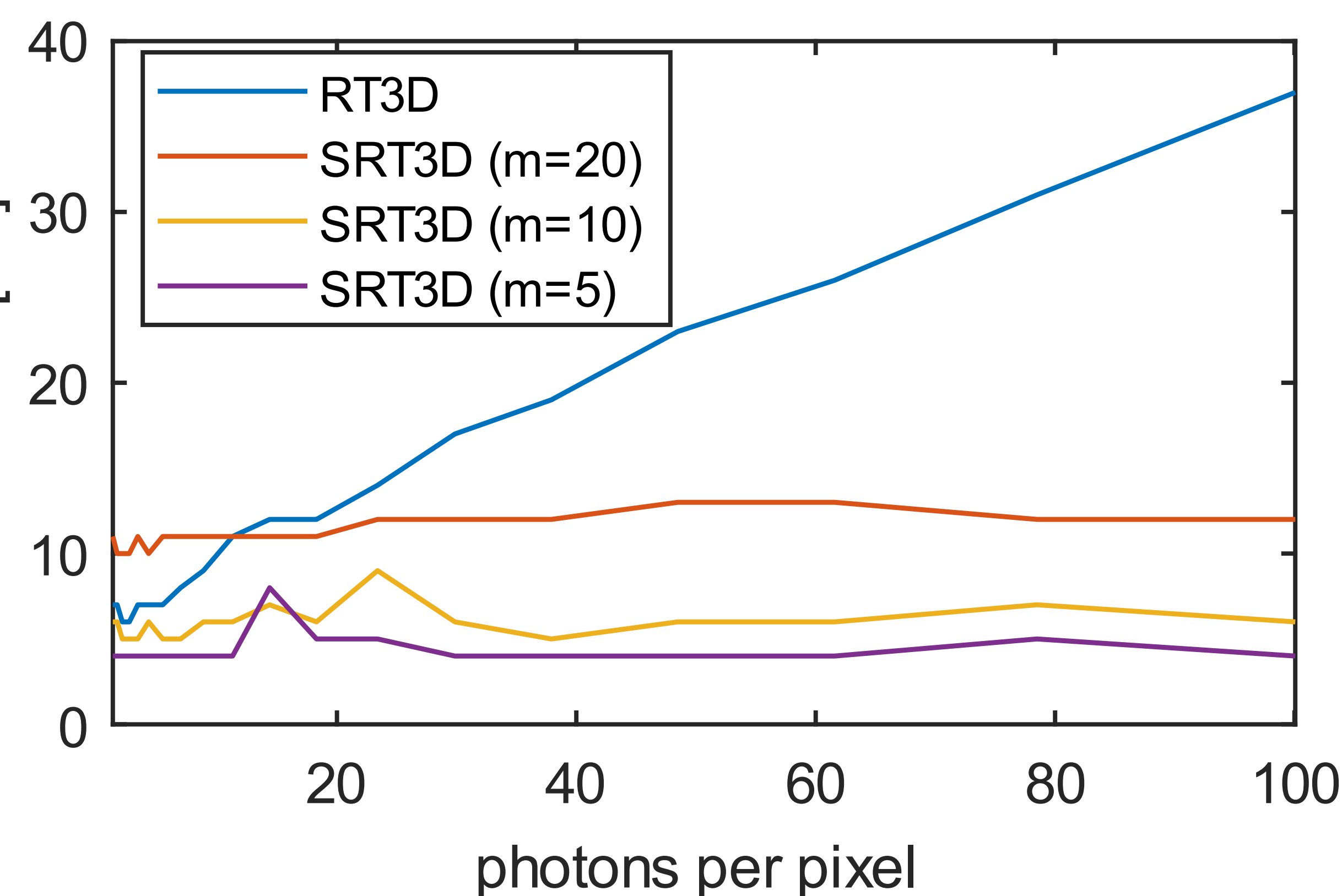
- Most reconstruction methods define some $\rho(\theta)$ to promote smooth reconstructions [1]
 - We choose RT3D which is real-time and multi-surface [2]
- REFLECTIVITY + DEPTH PARAMETERS

	Histogram-based $y \in \mathbb{R}^T$	Sketched-based (ours) $z \in \mathbb{R}^{2m}$
Pixelwise Statistics	$y_\ell = \sum_{p=1}^n \mathbf{1}_{x_p \in [t_\ell, t_\ell + \Delta t]}$ Poisson distrib.	$z_\ell = \frac{1}{n} \sum_{p=1}^n e^{i\omega_\ell x_p} \approx$ Gaussian distrib.
Reconstruction Objective	$\arg \min_{\theta} \sum_{i,j} f_{y_{i,j}}(\theta_{i,j}) + \rho(\theta)$	$\arg \min_{\theta} \sum_{i,j} \ z_{i,j} - \mathbb{E}_{\theta}\{z_{i,j}\}\ ^2 + \rho(\theta)$
Complexity	$\mathcal{O}(\min\{n, T\})$	$\mathcal{O}(\text{sketches})$

Advantages of sketching

- m (# sketches) $\approx K$ (# parameters) $\ll T$ (# bins)
- Computed **online** and **on-chip**
- Less computation
- Removes data transfer bottleneck

Experiments



[1] Rapp et al. "Advances in Single-Photon Lidar for Autonomous Vehicles: Working Principles, Challenges, and Recent Advances", IEEE SPM, 2020

[2] Tachella et al. "Real-time 3D reconstruction from single-photon lidar data using plug-and-play point cloud denoisers", Nature Communications, 2019